

## BALLARI INSTITUTE OF TECHNOLOGY & MANAGEMENT

(Autonomous Institute under Visvesvaraya Technological University, Belagavi)

USN

Course Code 2 1 E E 6 3

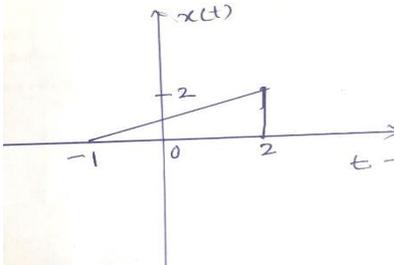
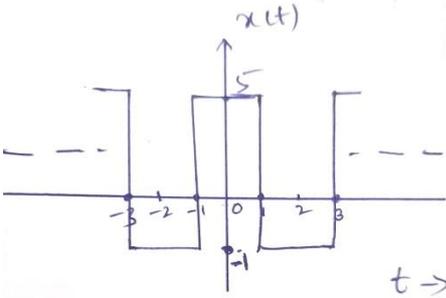
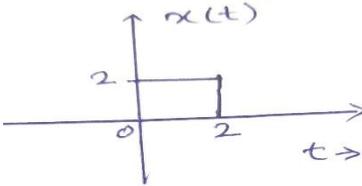
Sixth Semester B.E. Degree Examinations, September/October 2024

### SIGNALS & DIGITAL SIGNAL PROCESSING

Duration: 3 hrs

Max. Marks: 100

- Note:** 1. Answer any FIVE full questions choosing ONE full Question from each Module.  
2. Missing data, if any, may be suitably assumed

<u>Q.No</u>	<u>Question</u>	<u>Marks</u>	<u>(RBTL:CO:PI)</u>
<b>Module-1</b>			
1. a.	For the signal $x(t)$ is shown in Fig. Q 1(a), perform the following operation: (i) $x(t+3)$ (ii) $x(0.5t+2)$ (iii) $x(2-t)$	05	(3:1:1.3.1)
			<b>Fig.Q1(a)</b>
b.	Determine energy and power of the signal shown in Fig. Q1(b).	05	(3:1: 1.3.1)
			<b>Fig.Q1(b)</b>
c.	Determine whether the system $y(t) = \sin[x(t)]$ is linear, casual, time invariant, memoryless and stable.	05	(3:2:1.4.1)
d.	For the input signal $x(n) = (4, 2, 1, 5)$ and impulse response $h(n) = (2, 6, 4)$ Determine convolution sum $y(n) = x(n) * h(n)$	05	(3:2:1.4.1)
<b>(OR)</b>			
2. a.	Sketch the even and odd components of the signal shown in Fig. Q 2(a).	05	(3:1:1.4.1)
			<b>Fig.Q 2(a)</b>
b.	Determine whether the following signals are periodic or not. Find the period if periodic. (i) $x(t) = \sin(\pi/3)t \cos(\pi/4)t$ (ii) $x(n) = \cos \pi n$	05	(3:1:1.4.1)
c.	Determine whether the system $y(n) = \log[x(n)]$ is linear, casual, time invariant, memoryless and stable.	05	(3:2:1.4.1)

- d. Determine convolution integral  $y(t)=x(t)*h(t)$  where  $x(t)=e^{-3t}u(t)$  and  $h(t)=u(t-2)$  05 (3:2:1.4.1)

**Module-2**

- 3 a Obtain 4 point DFT of the sequence  $x(n)= (2,-3,5,1)$  . 06 (3:3:1.4.1)
- b Determine circular convolution of sequences  $x_1(n)= (1,0,2,5)$  and  $x_2(n)= (3,-4,1,6)$  using concentric circles method 06 (3:3:1.4.1)
- c A sequence  $x(n)= (2,5,-1,3,7,2,8,1,2,5,1,5)$  is filtered through a filter having impulse response  $h(n)=( 1,-1, 1)$ . Using overlap and save method determine output  $y(n)$  of the filter. Use 6 point circular convolution. 08 (3:3:1.4.1)
- (OR)

- 4 a Determine IDFT of  $X(k)=(3, 2+j, 1, 2-j)$  06 (3:3:1.4.1)
- b Obtain the DFT of  $x(n)=(6,2,-3,4)$ . Using circular time shift property obtain DFT of  $x((n-1))_4$  06 (3:3:1.4.1)
- c Determine the output  $y(n)$  of a filter having input  $x(n)= (1,-4,6,-2,3,1,5,2,7,2,4,-3)$  and impulse response  $h(n)=( 2,1,1)$  using overlap and add method. Use 5 point circular convolution. 08 (3:3:1.4.1)

**Module-3**

5. a. Using Radix-2 DIT-FFT algorithm, determine 8 point DFT of  $x(n)= [1,0,1,0,1,0,1,0]$  10 (3:3:1.4.1)
- b. Determine IDFT of  $X(k)= (7,-0.707-j0.707, -j, 0.707-j0.707, 1, 0.707+j0.707, j, -0.707+j0.707)$  using Radix-2 DIF-FFT algorithm. 10 (3:3:1.4.1)
- (OR)

6. a. Using Radix-2 DIF-FFT algorithm obtain the circular convolution of  $x_1(n)= ( 1,2,1,3)$  and  $x_2(n)= ( 2,0,2,0)$  10 (3:3:1.4.1)
- b. Obtain IDFT of  $X(k)= (2,0.5-j1.207, 0, 0.5-j0.207, 0, 0.5+0.207, 0.0.5+j1.207)$  using Radix-2 DIT-FFT algorithm 10 (3:3:1.4.1)

**Module-4**

7. a. Design a low pass Butterworth filter to meet the following specifications. 10 (3:4:1.4.1)  
 Pass band gain = -2 dB at  $\Omega_p = 20$  rad/sec  
 Stop band attenuation  $\geq 10$  dB at  $\Omega_s = 30$  rad/sec
- b. Using Bilinear transformation design a Butterworth low pass filter to satisfy following specifications: 10 (3:4:1.4.1)  
 $0.8 \leq |H(\omega)| \leq 1$  for  $0 \leq \omega \leq 0.2\pi$   
 $|H(\omega)| \leq 0.2$  for  $0.6\pi \leq \omega \leq \pi$
- (OR)

8. a. Design a Chebyshev filter to meet the following specifications: 10 (3:4:1.4.1)  
 Acceptable pass band ripple of 2.5 dB  
 Passband edge frequency of 20 rad/sec  
 Stop band attenuation of 30 dB or more at 50 rad/sec
- b. Using Impulse Invariant Technique, design a low pass filter to meet following specifications: 10 (3:4:1.4.1)  
 $20 \log |H(\omega)|_{\omega=0.2\pi} = -2$  dB  
 $20 \log |H(\omega)|_{\omega=0.6\pi} = -15$  dB  
 Filter must have approximately flat frequency response.

**Module-5**

9. a. The desired frequency response of a low pass filter is given by **10 (3:4:1.4.1)**  
$$H_d(\omega) = \begin{cases} e^{-j2\omega} & |\omega| \leq 3\pi/4 \\ 0 & 3\pi/4 \leq |\omega| \leq \pi \end{cases}$$

Determine filter coefficients of FIR filter using Hamming window. Also obtain the frequency response of FIR filter.

- b. Draw the direct form I, direct form II and cascade realizations for IIR filter described by the system function **10 (3:5:1.4.1)**

$$H(z) = \frac{(1 - \frac{1}{3}z^{-1})(1 + \frac{1}{8}z^{-1})}{(1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2})(1 + \frac{1}{2}z^{-1})}$$

**(OR)**

- 10 a. A filter is to be designed with following desired frequency response specifications: **10 (3:4:1.4.1)**  
$$H_d(\omega) = \begin{cases} 0 & -\pi/2 \leq \omega \leq \pi/2 \\ e^{-j3\omega} & \pi/2 \leq |\omega| \leq \pi \end{cases}$$

Determine the filter coefficients of FIR filter and the frequency response. Use rectangular window for the design.

- b. Realize the following system function in direct form and linear phase form **10 (3:5:1.4.1)**

$$H(z) = 1 + \frac{3}{7}z^{-1} + \frac{12}{17}z^{-2} + \frac{15}{8}z^{-3} + \frac{12}{17}z^{-4} + \frac{3}{7}z^{-5} + z^{-6}$$

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