

BALLARI INSTITUTE OF TECHNOLOGY & MANAGEMENT

(Autonomous Institute under Visvesvaraya Technological University, Belagavi)

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Course Code

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Sixth Semester B.E. Degree Examinations, September/October 2024

SIGNALS & DIGITAL SIGNAL PROCESSING

Duration: 3 hrs

Max. Marks: 100

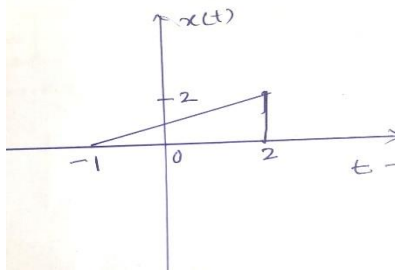
Note: 1. Answer any FIVE full questions choosing ONE full Question from each Module.

2. Missing data, if any, may be suitably assumed

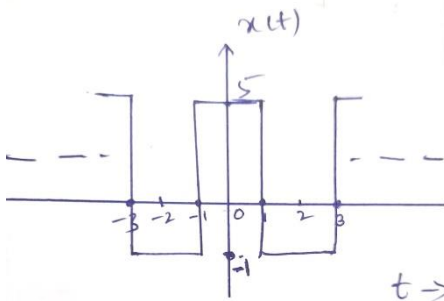
<u>Q.No</u>	<u>Question</u>	<u>Marks</u>	<u>(RBTL:CO:PI)</u>
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Module-1

1. a. For the signal $x(t)$ is shown in Fig. Q 1(a), perform the following operation:
 (i) $x(t+3)$ (ii) $x(0.5t+2)$ (iii) $x(2-t)$

**Fig.Q1(a)**

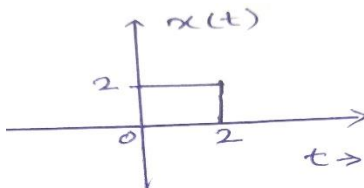
- b. Determine energy and power of the signal shown in Fig. Q1(b). 05 (3:1: 1.3.1)

**Fig.Q1(b)**

- c. Determine whether the system $y(t) = \sin[x(t)]$ is linear, casual, time invariant, memoryless and stable. 05 (3:2:1.4.1)
- d. For the input signal $x(n) = (4, 2, 1, 5)$ and impulse response $h(n) = (2, 6, 4)$ Determine convolution sum $y(n) = x(n) * h(n)$ 05 (3:2:1.4.1)

(OR)

2. a. Sketch the even and odd components of the signal shown in Fig. Q 2(a). 05 (3:1:1.4.1)

**Fig.Q 2(a)**

- b. Determine whether the following signals are periodic or not. Find the period if periodic.
 (i) $x(t) = \sin(\pi/3)t \cos(\pi/4)t$ (ii) $x(n) = \cos \pi n$ 05 (3:1:1.4.1)
- c. Determine whether the system $y(n) = \log[x(n)]$ is linear, casual, time invariant, memoryless and stable. 05 (3:2:1.4.1)

Note: (RBTL - Revised Bloom's Taxonomy Level: CO - Course Outcome: PI- Performance Indicator)

- d. Determine convolution integral $y(t)=x(t)*h(t)$ where $x(t)=e^{-3t}u(t)$ and $h(t)=u(t-2)$ 05 (3:2:1.4.1)

Module-2

- 3 a Obtain 4 point DFT of the sequence $x(n) = (2, -3, 5, 1)$. 06 (3:3:1.4.1)
- b Determine circular convolution of sequences $x_1(n) = (1, 0, 2, 5)$ and $x_2(n) = (3, -4, 1, 6)$ using concentric circles method 06 (3:3:1.4.1)
- c A sequence $x(n) = (2, 5, -1, 3, 7, 2, 8, 1, 2, 5, 1, 5)$ is filtered through a filter having impulse response $h(n) = (1, -1, 1)$. Using overlap and save method determine output $y(n)$ of the filter. Use 6 point circular convolution. 08 (3:3:1.4.1)
- (OR)

- 4 a Determine IDFT of $X(k) = (3, 2+j, 1, 2-j)$ 06 (3:3:1.4.1)
- b Obtain the DFT of $x(n) = (6, 2, -3, 4)$. Using circular time shift property obtain DFT of $x((n-1))_4$ 06 (3:3:1.4.1)
- c Determine the output $y(n)$ of a filter having input $x(n) = (1, -4, 6, -2, 3, 1, 5, 2, 7, 2, 4, -3)$ and impulse response $h(n) = (2, 1, 1)$ using overlap and add method. Use 5 point circular convolution. 08 (3:3:1.4.1)

Module-3

5. a. Using Radix-2 DIT-FFT algorithm, determine 8 point DFT of $x(n) = [1, 0, 1, 0, 1, 0, 1, 0]$ 10 (3:3:1.4.1)
- b. Determine IDFT of $X(k) = (7, -0.707-j0.707, -j, 0.707-j0.707, 1, 0.707+j0.707, j, -0.707+j0.707)$ using Radix-2 DIF-FFT algorithm. 10 (3:3:1.4.1)
- (OR)

6. a. Using Radix-2 DIF-FFT algorithm obtain the circular convolution of $x_1(n) = (1, 2, 1, 3)$ and $x_2(n) = (2, 0, 2, 0)$ 10 (3:3:1.4.1)
- b. Obtain IDFT of $X(k) = (2, 0.5-j1.207, 0, 0.5-j0.207, 0, 0.5+0.207, 0.0.5+j1.207)$ using Radix-2 DIT-FFT algorithm 10 (3:3:1.4.1)

Module-4

7. a. Design a low pass Butterworth filter to meet the following specifications. Pass band gain = -2 dB at $\Omega_p = 20$ rad/sec
Stop band attenuation ≥ 10 dB at $\Omega_s = 30$ rad/sec 10 (3:4:1.4.1)
- b. Using Bilinear transformation design a Butterworth low pass filter to satisfy following specifications:
 $0.8 \leq |H(\omega)| \leq 1$ for $0 \leq \omega \leq 0.2\pi$
 $|H(\omega)| \leq 0.2$ for $0.6\pi \leq \omega \leq \pi$ 10 (3:4:1.4.1)
- (OR)
8. a. Design a Chebyshev filter to meet the following specifications:
Acceptable pass band ripple of 2.5 dB
Passband edge frequency of 20 rad/sec
Stop band attenuation of 30 dB or more at 50 rad/sec 10 (3:4:1.4.1)
- b. Using Impulse Invariant Technique, design a low pass filter to meet following specifications:
 $20 \log |H(\omega)|_{\omega=0.2\pi} = -2$ dB
 $20 \log |H(\omega)|_{\omega=0.6\pi} = -15$ dB
Filter must have approximately flat frequency response. 10 (3:4:1.4.1)

Module-5

9. a. The desired frequency response of a low pass filter is given by **10 (3:4:1.4.1)**

$$H_d(\omega) = e^{-j2\omega} \quad \left| \omega \right| \leq 3\pi/4$$

$$= 0 \quad 3\pi/4 \leq \left| \omega \right| \leq \pi$$
Determine filter coefficients of FIR filter using Hamming window. Also obtain the frequency response of FIR filter.
- b. Draw the direct form I, direct form II and cascade realizations for IIR filter described by the system function **10 (3:5:1.4.1)**

$$H(z) = \frac{(1 - \frac{1}{3}z^{-1})(1 + \frac{1}{8}z^{-1})}{(1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2})(1 + \frac{1}{2}z^{-1})}$$
- (OR)**
- 10 a. A filter is to be designed with following desired frequency response specifications: **10 (3:4:1.4.1)**

$$H_d(\omega) = 0 \quad -\pi/2 \leq \omega \leq \pi/2$$

$$= e^{-j3\omega} \quad \pi/2 \leq \left| \omega \right| \leq \pi$$
Determine the filter coefficients of FIR filter and the frequency response. Use rectangular window for the design.
- b. Realize the following system function in direct form and linear phase form **10 (3:5:1.4.1)**

$$H(z) = 1 + \frac{3}{7}z^{-1} + \frac{12}{17}z^{-2} + \frac{15}{8}z^{-3} + \frac{12}{17}z^{-4} + \frac{3}{7}z^{-5} + z^{-6}$$

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