

BALLARI INSTITUTE OF TECHNOLOGY & MANAGEMENT

(Autonomous Institute under Visvesvaraya Technological University, Belagavi)

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Course Code

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First Semester B.E. Degree Examinations, March/April 2023 MATHEMATICS FOR CIVIL STREAM-I

Duration: 3 hrs

Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.
2. Missing data, if any, may be suitably assumed

<u>Q. No</u>	<u>Question</u>	<u>Marks</u>	<u>(RBTL:CO: PI)</u>
MODULE – 1			
1. a.	Find the rank of the matrix $A = \begin{bmatrix} 2 & 1 & 3 & 5 \\ 4 & 2 & 1 & 3 \\ 8 & 4 & 7 & 13 \\ 8 & 4 & -3 & -1 \end{bmatrix}$	06	2:1:1.2.1
b.	Test for consistency and solve : $x + 2y + 3z = 14$, $4x + 5y + 7z = 35$, $3x + 3y + 4z = 21$.	07	2:1:1.2.1
c.	Solve by Gauss elimination method . $x + 2y + z = 3$, $2x + 3y + 2z = 5$, $3x - 5y + 5z = 2$.	07	2:1:1.2.1
OR			
2. a.	Solve the following system of equation by Gauss-Jordan method . $2x_1 + x_2 + 3x_3 = 1$, $4x_1 + 4x_2 + 7x_3 = 1$, $2x_1 + 5x_2 + 9x_3 = 3$.	06	2:1:1.2.1
b.	Solve the following system of equation by Gauss-Seidel method. $10x + 2y + z = 9$, $x + 10y - z = -22$, $-2x + 3y + 10z = 22$.	07	2:1:1.2.1
c.	Find the largest eigen value and the corresponding eigen vector of the matrix A, by using the power method by taking initial vector $[1,1,1]^T$ $A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$	07	2:1:1.2.1
MODULE – 2			
3. a.	Prove with usual notations , $\tan \phi = r \left(\frac{d\theta}{dr} \right)$.	06	2:2:1.2.1
b.	Show that the following pairs of curves intersect each other orthogonally. $r = a(1 + \sin \theta)$ and $r = a(1 - \sin \theta)$.	07	2:2:1.2.1

- c. Find the pedal equation for the curve, $\frac{2a}{r} = (1 + \cos \theta)$. 07 2:2:1.2.1

OR

4. a. With usual notations prove that, $\rho = \frac{(1 + y_1^2)^{3/2}}{y_2}$. 06 2:2:1.2.1

- b. Find the radius curvature for the curve $r^n = a^n \cos n\theta$. 07 2:2:1.2.1

- c. Find ρ of the curve $y^2 = \frac{a^2(a-x)}{x}$ at the point $(a, 0)$. 07 2:2:1.2.1

MODULE – 3

5. a. Expand $e^{\sin x}$ as Maclaurin's series up to the terms containing x^4 . 06 2:3:1.2.1

- b. If $u = \log \sqrt{x^2 + y^2 + z^2}$, show that 07 2:3:1.2.1

$$(x^2 + y^2 + z^2) \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right) = 1.$$

- c. If $z(x+y) = x^2 + y^2$, show that $\left[\frac{\partial z}{\partial x} - \frac{\partial z}{\partial y} \right]^2 = 4 \left[1 - \frac{\partial z}{\partial x} - \frac{\partial z}{\partial y} \right]$. 07 2:3:1.2.1

OR

6. a. If $u = f\left(\frac{x}{y}, \frac{y}{z}, \frac{z}{x}\right)$, prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z} = 0$. 06 2:3:1.2.1

- b. Examine the function $f(x, y) = x^4 + y^4 - 2(x - y)^2$ for extreme values. 07 2:3:1.2.1

- c. If $x + y + z = u$, $y + z = uv$, and $z = uvw$, Show that $\frac{\partial(x, y, z)}{\partial(u, v, w)} = u^2 v$. 07 2:3:1.2.1

MODULE – 4

7. a. Solve: $ye^{xy} dx + (xe^{xy} + 2y) dy = 0$ 06 2:4:1.2.1

- b. Solve: $(x^3 + y^2 + x) dx + xy dy = 0$. 07 2:4:1.2.1

- c. Solve: $r \sin \theta - \cos \theta \frac{dr}{d\theta} = r^2$. 07 3:4:1.2.1

OR

8. a. Find the orthogonal trajectories of the family $y^2 = cx^3$. 06 2:4:1.2.1

- b. A series circuit with resistance R, inductance L and electromotive force E is generated by the differential equation $L \frac{di}{dt} + Ri = E$, where L and R are constants and initially the current i is zero. Find the current at any time t. 07 3:4:1.2.1

- c. Solve : $xy\left(\frac{dy}{dx}\right)^2 - (x^2 + y^2)\frac{dy}{dx} + xy = 0.$ 07 2:4:1.2.1

MODULE – 5

9. a. Evaluate : $\int_0^1 \int_0^{\sqrt{1-x^2}} \int_0^{\sqrt{1-x^2-y^2}} xyz \, dz \, dy \, dx$ 06 2:5:1.2.1

- b. Change the order of integration and hence evaluate $\int_0^{4a} \int_{x^2/4a}^{2\sqrt{ax}} xy \, dy \, dx.$ 07 2:5:1.2.1

- c. Find by double integration the area enclosed by the curve $r = a(1 + \cos \theta)$ between $\theta = 0$ and $\theta = \pi$. 07 3:5:1.2.1

OR

10. a. Find the volume of the solid bounded by the planes $x = 0, y = 0, z = 0,$ $x = y + z = 1.$ 06 2:5:1.2.1

- b. Prove that : $\beta(m, n) = \frac{\overline{m} \overline{n}}{\overline{m+n}}.$ 07 2:5:1.2.1

- c. Show that : $\int_0^{\pi/2} \frac{d\theta}{\sqrt{\sin \theta}} \times \int_0^{\pi/2} \sqrt{\sin \theta} \, d\theta = \pi.$ 07 3:5:1.2.1

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