

BALLARI INSTITUTE OF TECHNOLOGY & MANAGEMENT

(Autonomous Institute under Visvesvaraya Technological University, Belagavi)

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Course Code

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Second Semester B.E. Degree Examinations, September/October 2023 Mathematics for EEE Stream- II

Duration: 3 hrs

Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.
2. Missing data, if any, may be suitably assumed

<u>Q. No</u>	<u>Question</u>	<u>Marks</u>	<u>(RBTL:CO:PI)</u>
MODULE - 1			
1.	a. Find the directional derivatives of $\phi = x^2yz + 4xz^2$ at $(1, -2, -1)$ along $2i - j - 2k$	06	1:1:1.2.1
	b. Show that $\vec{F} = \frac{xi+yj}{x^2+y^2}$ is both solenoidal and irrotational	07	3:1:1.2.1
	c. If $\vec{r} = xi + yj + zk$ and $r = \vec{r} $ prove that $\nabla^2(r^n) = n(n+1)r^{n-2}$	07	3:1:1.2.1
OR			
2.	a. Find the total work done by the force represented by $\vec{F} = 3xyi - yj + 2zjk$ in moving a particle round the circle $x^2 + y^2 = 4$	06	1:1:1.2.1
	b. Verify Green's theorem in a plane for $\int (3x^2 - 8y^2)dx + (4y - 6xy)dy$, where C is the boundary of the region enclosed by $y = \sqrt{x}$ and $y = x^2$	07	3:1:1.2.1
	c. Verify Stoke's theorem for $\vec{F} = (2x - y)i - yz^2j - y^2zk$ where S is the upper half surface of the sphere $x^2 + y^2 + z^2 = 1$, C is its boundary.	07	3:1:1.2.1
MODULE - 2			
3.	a. Solve $(D^4 + 4D^3 - 5D^2 - 36D + 36)y = 0$	06	3:2:1.2.1
	b. Solve $\frac{d^2y}{dx^2} - 4y = \cosh(2x - 1) + 3^x$	07	3:2:1.2.1
	c. Solve $x^3 \frac{d^3y}{dx^3} + 3x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + 8y = 65 \cos(\log x)$	07	3:2:1.2.1
OR			
4.	a. Solve $\frac{d^3y}{dx^3} + 2 \frac{d^2y}{dx^2} + \frac{dy}{dx} = e^{-x} + \sin 2x$	06	3:2:1.2.1
	b. Use the method of variations of parameters to solve $\frac{d^2y}{dx^2} + y = \frac{1}{1 + \sin x}$	07	3:2:1.2.1
	c. Solve $(2x + 1)^2 y'' - 6(2x + 1)y' + 16y = 8(2x + 1)^2$	07	3:2:1.2.1

MODULE – 3

5. a. Find the Laplace transform of the following functions 06 1:3:1.2.1
- i) $3\sqrt{t} + \frac{4}{\sqrt{t}}$ ii) $\frac{1-e^{-at}}{t}$

- b. Find the Laplace transform of the full wave rectifier 07 1:3:1.2.1

$$f(t) = E \sin wt, \quad 0 < t < \pi/w \text{ having period } \frac{\pi}{w}$$

- c. Express the function $f(t) = \begin{cases} \sin t, & 0 < t \leq \frac{\pi}{2} \\ \cos t, & t > \frac{\pi}{2} \end{cases}$ in terms of 07 2:3:1.2.1

Heaviside unit step function and hence find their Laplace transform.

OR

6. a. Find the inverse Laplace transform of $\frac{4s+5}{(s+1)^2(s+2)}$ 06 1:3:1.2.1

- b. Find $L^{-1}\left[\frac{1}{(s+1)(s^2+1)}\right]$ using Convolution theorem. 07 1:3:1.2.1

- c. Solve the following initial value problem by using Laplace transforms: $\frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 4y = e^{-t}; y(0) = 0, y'(0) = 0$ 07 3:3:1.2.1

MODULE – 4

7. a. Compute a real root of $x \log_{10} x - 1.2 = 0$ by the method of false position. Carry out three iterations. 06 3:4:1.2.1

- b. Find the number of students from the following table who have obtained (i) less than 45 marks (ii) between 40 and 45 marks. By using interpolation formula. 07 1:4:1.2.1

Marks	30-40	40-50	50-60	60-70	70-80
No. of students	31	42	51	35	31

- c. Find $\sin 57^\circ$ using an appropriate interpolation formula, given $\sin 45^\circ = 0.7071$, $\sin 50^\circ = 0.7660$, $\sin 55^\circ = 0.8192$, $\sin 60^\circ = 0.8660$ 07 1:4:1.2.1

OR

8. a. Use Lagrange's interpolation formula to find $f(4)$ given 06 3:4:1.2.1

x	0	2	3	6
f(x)	-4	2	14	158

- b. Use trapezoidal rule to estimate $\int_0^2 e^{x^2} dx$ taking 10 intervals 07 3:4:1.2.1

- c. Evaluate $\int_0^6 \frac{dx}{1+x^2}$ by using Simpson's $\left(\frac{1}{3}\right)^{rd}$ rule, by considering seven ordinates. 07 3:4:1.2.1

MODULE – 5

9. a. Use Taylor's series method to find $y(4.1)$ given that $\frac{dy}{dx} = \frac{1}{x^2+y}$ and $y(4) = 4$ 06 3:5:1.2.1
- b. Find y at $x=1.2$ taking $h=0.2$, Given $\frac{dy}{dx} = 1 + \frac{y}{x}$, $y=2$ at $x=1$, by applying modified Euler's method. 07 1:5:1.2.1
- c. Apply Milne's method to compute $y(1.4)$ correct to 4 decimal places given $\frac{dy}{dx} = x^2 + \frac{y}{2}$ and the following data: $y(1) = 2$, $y(1.1) = 2.2156$, $y(1.2) = 2.4649$, $y(1.3) = 2.7514$ 07 3:5:1.2.1
- OR**
10. a. Solve: $(y^2 - x^2)dx = (y^2 + x^2)dy$ for $x=0.2$ given that $y=1$ at $x=0$ by applying R-K method of order 4 06 3:5:1.2.1
- b. Using Modified Euler's method find $y(20.2)$ given that $\frac{dy}{dx} = \log_{10}\left(\frac{x}{y}\right)$ with $y(20) = 5$ and $h=0.2$ 07 3:5:1.2.1
- c. Using scilab develop a program to solve ODE using R-K fourth order method for $f = x^2 + y^2$ with the conditions $x_0 = 1, y_0 = 1.2, x_f = 1.1, h = 0.01$ 07 3:5:1.2.7

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